

## Chapter 3: Patterns, Relations, Equations and Predictions

- Describing Patterns
- Solving Equations (algebra)
- $y = mx + b$

### Section 3.1 - Describing Patterns

Curriculum Outcomes	Related Activities	Page in Text
<ul style="list-style-type: none"> <li>express problems in terms of equations and vice versa</li> <li>model real-world phenomena with linear, quadratic, exponential, and power equations</li> <li>gather data, plot the data using appropriate scales, and demonstrate an understanding of independent and dependent variables and domain and range</li> <li>construct and analyze tables relating two variables</li> <li>develop and apply strategies for solving problems</li> <li>describe real-world relationships depicted by graphs and tables of values</li> <li>identify, generalize, and apply patterns</li> <li>solve problems using graphing technology</li> <li>determine if a graph is linear by plotting points in a given situation</li> </ul>	<ul style="list-style-type: none"> <li>investigations on gathering data about visible faces on cube "trains"</li> <li>a Focus on graphing data and using data to make predictions</li> <li>develop an equation in the form <math>ax + b = c</math></li> <li>demonstrate and apply an understanding of discrete and continuous number systems</li> </ul>	<p>96</p> <p>97</p> <p>98</p> <p>101</p>

## THE NUMBER SYSTEM

W = Whole Numbers

I = Integers

$\bar{Q}$  = Irrational Numbers

R = Real Numbers

N = Natural Numbers

Q = Rational Numbers

### EXAMPLES:

W: 0, 1, 2, 3, ...

$\bar{Q}$ :  $\pi$  (3.141592...),  $\sqrt{3}$ , 1.23456738...,  $\sqrt{15}$ , ...

N: 1, 2, 3, ...

I: ..., -3, -2, -1, 0, 1, 2, 3, ...

R:  $-\frac{1}{2}$ ,  $\sqrt{15}$ , 0, -3, 3,  $\pi$  (3.141592), ...

Q:  $\frac{1}{2}$ ,  $-\frac{1}{2}$ ,  $\frac{11}{3}$ , 0.2, -0.2, 3, -3, 0, ...

### • Definitions

- Real numbers (R): ALL numbers; rational & irrational
- Irrational numbers ( $\bar{Q}$ ):
  - they cannot be written as a fraction
  - non-repeating decimal
  - non-terminating decimal
  - Examples: 0.2163875943.... and  $\pi$
- Rational numbers (Q):
  - a number that can be written as a fraction
  - Any number that is not an irrational number
  - Examples: -2.34,  $3.\overline{456}$ , 6.323 232 32...

## Definitions continued...

- Integers (I):
  - Positive and negative whole numbers
  - NO decimals
  - Examples: -400, +8, 0, 29, -49578
- Whole numbers (W):
  - all of the positive integers and zero
  - Examples: 0, 1, 2, 3, 4, etc.
  - NO decimals
- Natural numbers (N):
  - all of the positive integers
  - DOES NOT include zero (only difference from whole numbers)
  - Examples: 1, 2, 3, 4, etc.

Using the previous definitions, determine if the following statements are sometimes true, always true, or never true. Justify your choices.

- A) All whole numbers are integers *Always*
- B) All integers are whole numbers *Sometimes*  
*-1, 0, 1*
- C) If a number is an integer then it is also a rational number. *Always*
- D) If a number is a rational number then it is also an integer. *Sometimes*  
*4 3.2*
- E) There is a number which is both rational and irrational. *Never*

### Copy and complete the table:

For each of the following numbers in the table, put an "x" in each category that the number belongs to. It may only belong in one, but could also belong to 5 out of the 6 categories. The first one is done for you.

Number	Real	Rational	Irrational	Whole	Natural	Integer
3.2	x	x				
0						
5.66						
-7						
15						
20009						
4.569...						
3.14...						
-3.22						
4/5						
14/2						
-6/3						
5/2						
-4.567...						
-23						
10						

Please double check your answers to make sure that you marked the appropriate boxes.

Number	Real	Rational	Irrational	Whole	Natural	Integer
3.2	X	X				
0	X	X		X		X
5.66	X	X				
-7	X	X				X
15	X	X		X	X	X
20009	X	X		X	X	X
4.569...	X		X			
3.14...	X		X			
-3.22	X	X				
4/5	X	X				
14/2	X	X		X	X	X
-6/3	X	X				X
5/2	X	X				
-4.567...	X		X			
-23	X	X				X
10	X	X		X	X	X

## Set Notation:

- We need to know what these signs mean:

such that  $\rightarrow$  |  
less than  $\rightarrow$  <  
greater than  $\rightarrow$  >  
less than or equal to  $\rightarrow$  ≤  
greater than or equal to  $\rightarrow$  ≥  
belongs to  $\rightarrow$  ∈

- We need to know what number type we are dealing with:

Natural Number = **N**

Whole Numbers = **W**

Integer = **I**

Rational Numbers = **Q**

Irrational Numbers =  **$\overline{Q}$**

Real Numbers = **R**

- Example:

$$\{x / x \leq 5, x \in I\}$$

## Set Notation:

- We need to know what these signs mean:

such that  $\rightarrow$  |  
less than  $\rightarrow$  <  
greater than  $\rightarrow$  >  
less than or equal to  $\rightarrow$  ≤  
greater than or equal to  $\rightarrow$  ≥  
belongs to  $\rightarrow$  ∈

- We need to know what number type we are dealing with:

Natural Number = **N**

Whole Numbers = **W**

Integer = **I**

Rational Numbers = **Q**

Irrational Numbers =  **$\overline{Q}$**

Real Numbers = **R**

- Example:

$$\{x / x \leq 5, x \in I\}$$

↑  
Variable  
(x)

↑  
x is  
less than  
or equal to 5

↑  
x belongs to  
Integers

Possible answers: 4, 5, 3, 0, -2

What if we were to graph this on a number line?

~~R~~ W

Ask Yourself:

• What set of numbers am I dealing with?

• What is the sign?: am I going right or left?

• Dots or a line?:

Dots

Lines

Integers

Real

Natural

Irrational

Whole

Rational

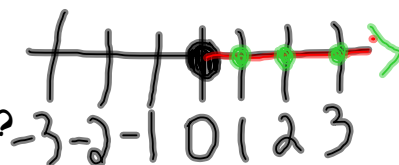
• Solid or open dots?:

Solid

Open

- if it can be  
equal to

- If that number isn't  
included

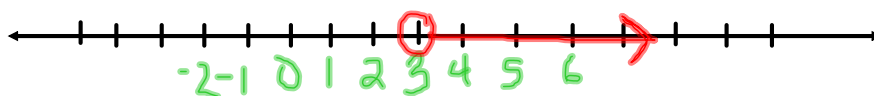


$$\{x / x \leq 5, x \in \textcircled{I}\}$$



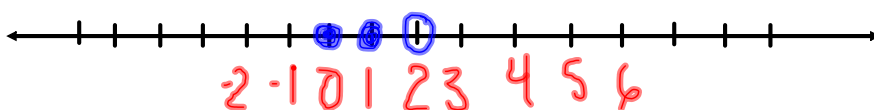
Example #2:

$$\{x / x > 3, x \in R\}$$



Example #3:

$$\{x / x < 2, x \in W\}$$



← dots

## Class work / Homework:

Copy and Complete the following:

### Section 3.1 - "Graphing Number Lines"

1. What set of numbers do the following represent?

- a)  $\mathbb{N}$       b)  $\overline{\mathbb{Q}}$       c)  $\mathbb{Q}$       d)  $\mathbb{R}$       e)  $\mathbb{W}$       f)  $\mathbb{I}$

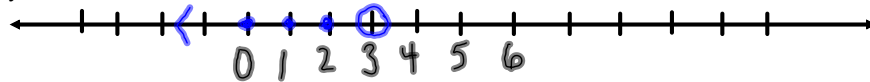
2. Graph the following on a number line. Use a ruler to draw the line.

- |   |   |  |
|---|---|--|
| a) $\{x / x < 3, x \in \mathbb{I}\}$    | b) $\{x / x < 3, x \in \mathbb{R}\}$    | c) $\{x / x \geq 2, x \in \mathbb{N}\}$                                      |
| d) $\{x / x \geq 2, x \in \mathbb{I}\}$ | e) $\{x / x < -3, x \in \mathbb{R}\}$   | f) $\{x / x < -3, x \in \mathbb{I}\}$  |
| g) $\{x / x < 4, x \in \mathbb{W}\}$    | h) $\{x / x \geq 0, x \in \mathbb{R}\}$ | i) $\{x / 0 < x \in \mathbb{I}\}$ <span style="color: blue;">x &gt; 0</span> |
| j) $\{x / 0 < x, x \in \mathbb{R}\}$    | k) $\{x / 9 > x, x \in \mathbb{R}\}$    | l) $\{x / 9 > x, x \in \mathbb{N}\}$   |

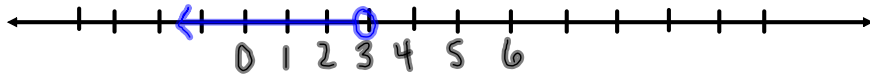
-1 0 . . .

## Answers:

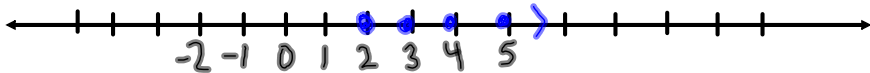
a)  $\{x / x < 3, x \in \mathbb{I}\}$



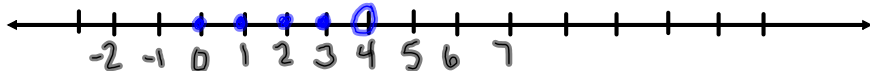
b)  $\{x / x < 3, x \in \mathbb{R}\}$



c)  $\{x / x \geq 2, x \in \mathbb{N}\}$

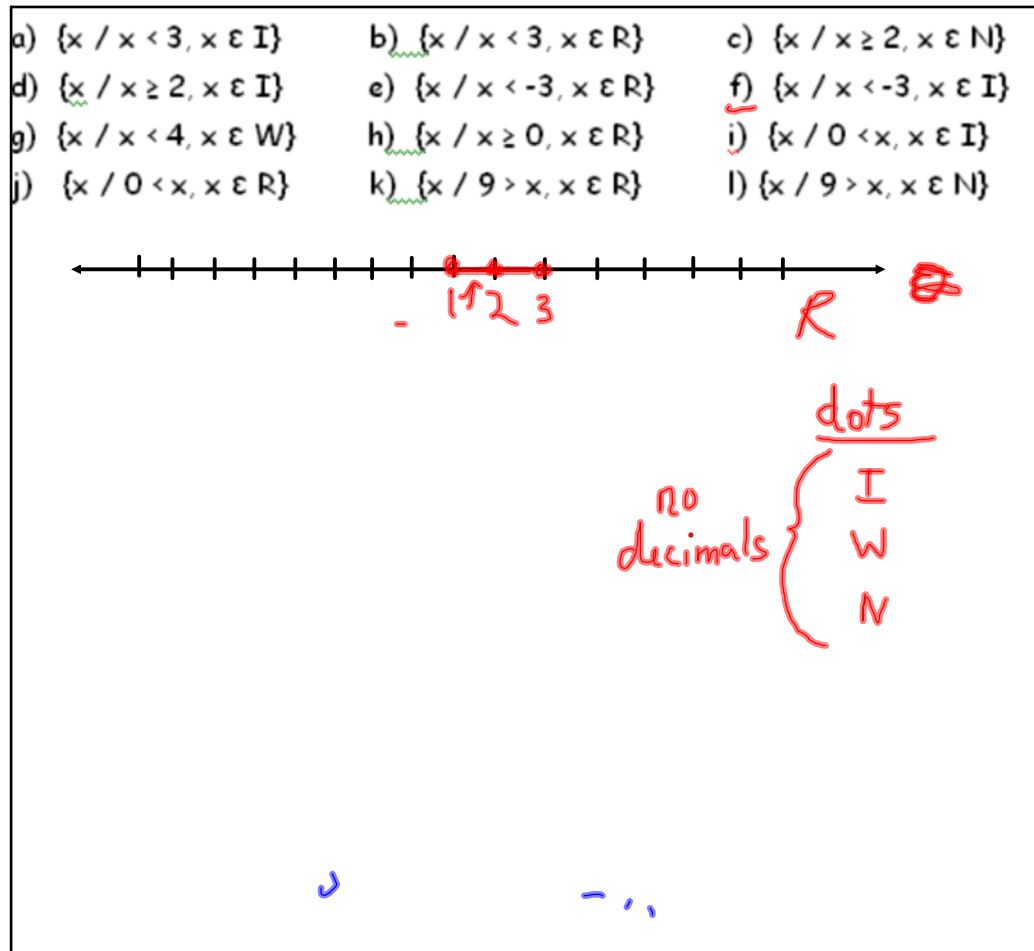


g)  $\{x / x < 4, x \in \mathbb{W}\}$



No arrow and  
no dots on the negatives  
because whole numbers  
are not negative.

f,



State what type of number system each of the following sets of numbers would fall under:

- a)  $\{-2, -1, 0, 3, 5, 7\}$  **R Q I**  
 b)  $\{-4.5, -2, -0.5, 0, 0.5, 6\}$  **R Q**  
 c)  $\{0, 2, 4, 6, 8\}$  **R Q I W**  
 d)  $\{2, 4, 6, 8, 10, 12\}$  **R Q N W I**  
 e)  $\{1/2, 1/4, 0.75\}$  **R Q**  
 f)  $\{\pi, \sqrt{2}, 5.482957271615303846202784\}$

**R Q**

**R**

**Q or Q**

**I, W, N No decimals**



10

### Warm Up: #10

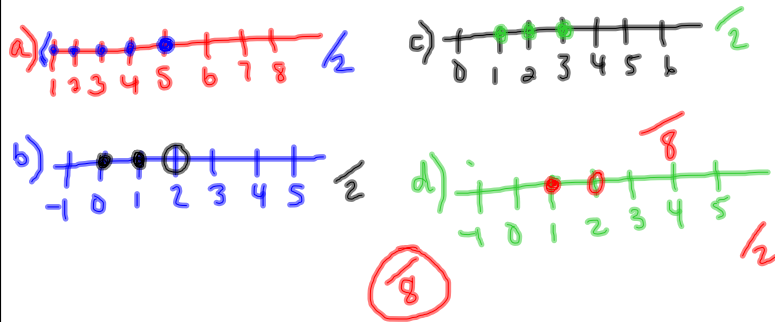
1. State what type of number system each of the following sets of numbers would fall under:

- a)  $\{-2, -1, 0, 3, 5, 7\}$
- b)  $\{-4.5, -2, -0.5, 0, 0.5, 6\}$
- c)  $\{0, 2, 4, 6, 8\}$
- d)  $\{2, 4, 6, 8, 10, 12\}$
- e)  $\{1/2, 1/4, 0.75\}$
- f)  $\{\pi, \sqrt{2}, 5.482957271615303846202784\}$

2. Graph the following on a number line:

a)  $\{x / x \leq 5, x \in \mathbb{I}\}$       b)  $\{x / x < 2, x \in \mathbb{W}\}$

c)  $\{x / x \leq 3, x \in \mathbb{N}\}$       d)  $\{x / x < 2, x \in \mathbb{N}\}$



10

### Warm Up: #10

1. State what type of number system each of the following sets of numbers would fall under:

- a)  $\{-2, -1, 0, 3, 5, 7\}$   $\mathbb{R} \mathbb{Q} \mathbb{I}$
- b)  $\{-4.5, -2, -0.5, 0, 0.5, 6\}$   $\mathbb{R} \mathbb{Q}$
- c)  $\{0, 2, 4, 6, 8\}$   $\mathbb{R} \mathbb{Q} \mathbb{I} \mathbb{W}$
- d)  $\{2, 4, 6, 8, 10, 12\}$   $\mathbb{R} \mathbb{Q} \mathbb{I} \mathbb{W} \mathbb{N}$
- e)  $\{1/2, 1/4, 0.75\}$   $\mathbb{R} \mathbb{Q}$
- f)  $\{\pi, \sqrt{2}, 5.482957271615303846202784\}$   $\mathbb{R} \bar{\mathbb{Q}}$

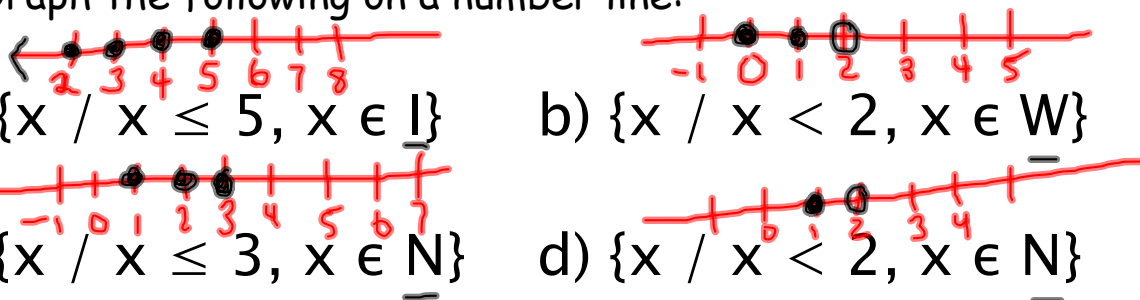
2. Graph the following on a number line:

a)  $\{x / x \leq 5, x \in \mathbb{I}\}$

b)  $\{x / x < 2, x \in \mathbb{W}\}$

c)  $\{x / x \leq 3, x \in \mathbb{N}\}$

d)  $\{x / x < 2, x \in \mathbb{N}\}$



## Modeling:

- a technique of producing a mathematical description or model that can be used to solve a practical problem
- modeling can be done through the use of:

### 1. Equations

Example:  $y = 2x$

### 2. Table of values

Example:

x	y
0	0
1	2
2	4
3	6

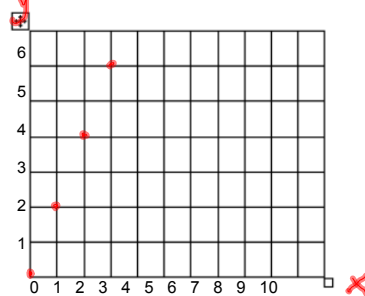
$(0,0)$   
 $(1,2)$

### 3. Ordered Pairs

Example:  $(0,0)$   $(1,2)$   $(2,4)$   $(3,6)$

### 4. Graphing

Example:



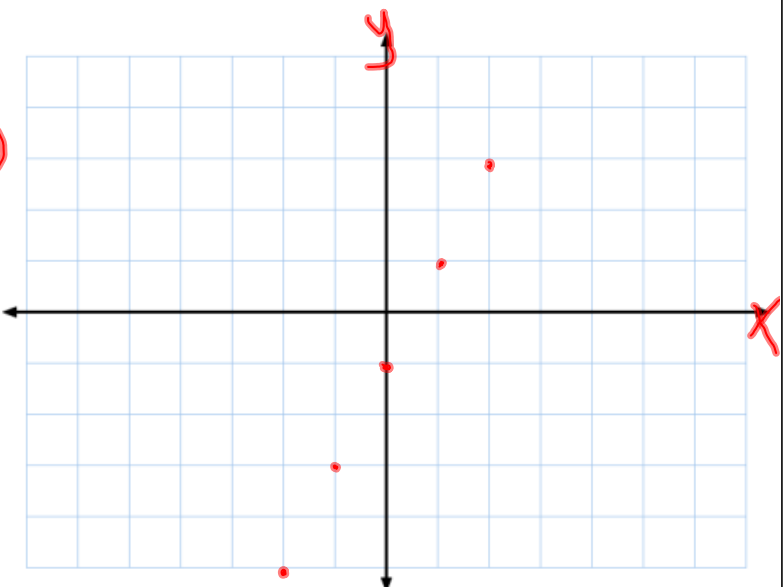
## Graphing Review:

Graph the following:  $y = 2x - 1$   $x, y \in \mathbb{R}$

### 1. Table of Values:

x	y
-2	-5
-1	-3
0	-1
1	1
2	3

$(-2,-5)$   
 $(-1,-3)$   
 $(0,-1)$   
 $(1,1)$   
 $(2,3)$



### 2. Graph the co-ordinates:

## Domain & Range:

Domain - set of all possible x values

Range - set of all possible y values

- When writing domain and range in set notation they should be written in order of smallest to largest. Numbers should not be repeated.

What is the domain for the following ordered pairs? What is the range?

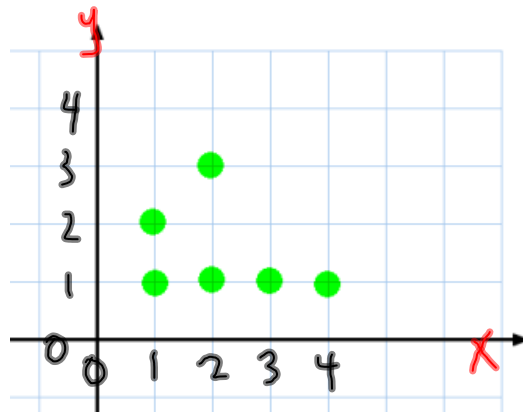
$(2,1) (3,4) (5,6) (8,9) (10,11)$  ←  $(3,9)$

Domain =  $2, 3, 5, 8, 10$

Range =  $1, 4, 6, 9, 11$

What is the domain for the following graph? What is the range?

$(x,y) \rightarrow$  always this order.



- least to greatest  
- can't repeat #'s

Domain<sup>x</sup> =  $1, 2, 3, 4$

Range<sup>y</sup> =  $1, 2, 3$

## Discrete & Continuous:

### Discrete Data

- finite number of values in between 2 points
- every number is not possible
- easily "countable"
- dots on a graph

Examples:

- o Number of books on a shelf
- o Number of defective items in a shipment of 50 pens

W, N, I  
- - - - -  
          ↑  
\_\_\_\_\_

### Continuous Data

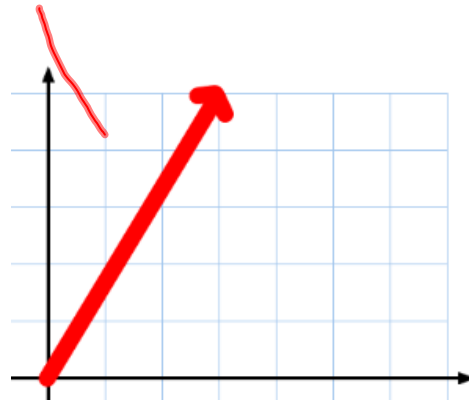
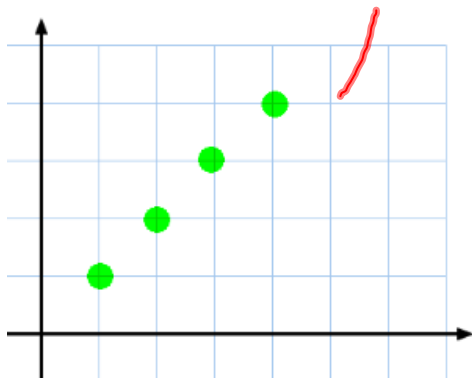
- infinite number of values in between 2 points
- every number is possible
- dots are joined

Examples:

- o 1-5 and everything in between
- timing for a 100 m dash

R  
\_\_\_\_\_

Is this a graph of Discrete or Continuous Data?



## Practice:

1. What is the domain & range of the following set of ordered pairs?

(2,1) (3,2) (8,9) (3,10) (1,3) (3,6) (2,10)

2. Are the following situations discrete or continuous?

- a) The height of trees at a nursery over a period of 20 years C
- b) The number of correct answers on a student's multiple choice quiz D
- c) How many times it would take a person to pass their driver's test D
- d) The length of time it takes for a light bulb to burn out C

$$\cancel{2x} - y = 2$$

$-2x$        $-2x$

Example

$$y = \underline{\quad} x + \underline{\quad}$$

$$x, y \in \underline{\quad}$$

$$\cancel{-1}y = -2x + 2$$

$-1$        $-1$

$$y = \underline{2x - 2}$$

x	y
0	-2
1	0
2	2
3	4
4	6

~~(0, -2)~~ (1, 0) (2, 2)  
 (3, 4) (4, 6)

$$\begin{aligned}
 &2x - 2 \\
 &2(0) - 2 \\
 &0 - 2 \\
 &-2 \\
 &2(1) - 2 \\
 &2 - 2 \\
 &= 0
 \end{aligned}$$

## Class work / Homework:

Complete worksheet:

"Section 3.1 - Domain & Range, Discrete & Continuous"

Domain, Range, Continuous & Discrete worksheet #2.doc

## Questions:

1. List the domain and range in set notation for each of the following sets of ordered pairs.

a)  $\{(2,1), (-1, 3), (4, 2), (3,-2)\}$

b)  $\{(0,2), (-1,-1), (3,2), (2,3)\}$

$$d = \{x \mid x = -1, 2, 3, 4, x \in \mathbb{I}\}$$

$$d = \{x \mid x = -1, 0, 2, 3, x \in \mathbb{I}\}$$

$$r = \{y \mid y = -2, 1, 2, 3, y \in \mathbb{I}\}$$

$$r = \{y \mid y = -1, 2, 3, y \in \mathbb{I}\}$$

2. List the domain and range in set notation for the table of values.

X	3	3	4	5	3	4	5	4	5	5
Y	1	1	1	1	2	2	2	3	3	4

$$\{x \mid x = 3, 4, 5, x \in \mathbb{N}\}$$

$$\{y \mid y = 1, 2, 3, 4, y \in \mathbb{N}\}$$

3. List the domain and range in set notation for each of the following graphs.

a)  $\{x | x = -1, 0, 1, 2, 3\}$   
 $\{y | y = 1, 2, 3, 4, 5\}$

b)  $x \in \mathbb{R}$   
 $y \in \mathbb{R}$

c)  $\{x | x = 0, 1, 2, 3, 4\}$   
 $\{y | y = 1, 2, 3, 4, 5\}$

4. Graph the following equations by creating a table of values. Determine if the data is either discrete or continuous.

a)  $x + y = 4$   $x, y \in \mathbb{R}$   $\mathbb{R}$   
 b)  $x + y = 3$   $x, y \in \mathbb{I}$   
 c)  $x + y = 2$   $x, y \in \mathbb{R}$   $\mathbb{R}$   
 d)  $x - y = 2$   $x, y \in \mathbb{R}$   $\mathbb{R}$

a)  $x + y = 4$   
 $-x$   

x	y = -x + 4	y
1	-1 + 4	3
2	-2 + 4	2
3	-3 + 4	1
4	-4 + 4	0
5	-5 + 4	-1

Coordinates: (1, 3), (2, 2), (3, 1), (4, 0), (5, -1) \* don't graph (5, -1) as  $\mathbb{N}$  not  $\mathbb{N}^+$

discrete or continuous  
 Why?  $\mathbb{N}$  - No decimals

b)  $x + y = 3$   $x, y \in \mathbb{I}$   
 $-x$   
 $y = -x + 3$   

x	y = -x + 3	y
-2	-(-2) + 3	5
-1	-(-1) + 3	4
0	0 + 3	3
1	-1 + 3	2
2	-2 + 3	1

Coordinates: (-2, 5), (-1, 4), (0, 3), (1, 2), (2, 1)

c)  $x + y = 2$   $x, y \in \mathbb{R}$   $\mathbb{R}$   
 $-x$   
 $y = -x + 2$   

x	y = -x + 2	y
-2	-(-2) + 2	4
-1	-(-1) + 2	3
0	0 + 2	2
1	-1 + 2	1
2	-2 + 2	0

Coordinates: (-2, 4), (-1, 3), (0, 2), (1, 1), (2, 0)

d)  $x - y = 2$   $x, y \in \mathbb{R}$   $\mathbb{R}$   
 $-x$   
 $-y = -x + 2$   
 $y = x - 2$   

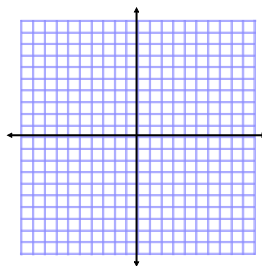
x	y = x - 2	y
-2	-2 - 2	-4
-1	-1 - 2	-3
0	0 - 2	-2
1	1 - 2	-1
2	2 - 2	0

Coordinates: (-2, -4), (-1, -3), (0, -2), (1, -1), (2, 0)

Example 1: Make a table of values and graph  
 $y = 4x - 5$   $x, y \in \mathbb{I}$  \*x\* values must be:

x	y = 4x - 5	y
-2	$y = 4(-2) - 5$	

Coordinates:



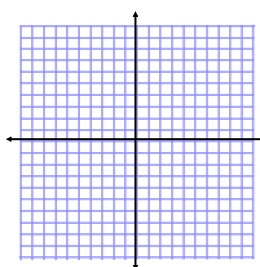
Example 2:  $x - y = 5$   $x, y \in \mathbb{W}$

- You need to rearrange this so that it is  $y =$  \_\_\_\_

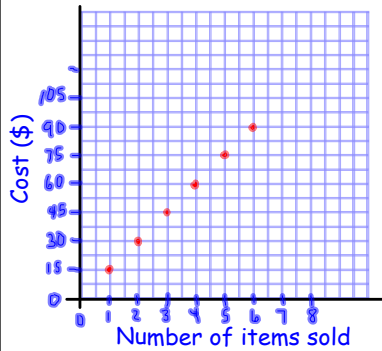
$$x - y = 5$$

x	y
---	---

Coordinates:



## Warm-Up #11



1. What is the independent variable?
2. What is the dependent variable?
3. What is the domain? write in set notation
4. What is the range? write in set notation
5. Would you connect these dots?
6. What type of data is this?
7. What type of numbers are these? List all that apply.

$$\{x \mid x \geq 0, x \in \mathbb{W}\}$$

### Class work / Homework:

For each of the following make a table of values and graph the coordinates. Copy these down.

(1)  $y = -2x - 1$

$x, y \in \mathbb{I}$

*dots D*

*continuous or discrete*

(2)  $y = 3x + 2$

$x, y \in \mathbb{W}$

*dots D*

(3)  $y = -1x - 2$

$x, y \in \mathbb{N}$

*dots D*

*Not plotted*

(4)  $x + y = -2$

$x, y \in \mathbb{R}$

*line C*

(5)  $-5y + 5x = 10$

$x, y \in \mathbb{I}$

*dots D*

*(5)  $-5y + 5x = 10$*

*(4)  $x + y = -2$*

$x$	$y = -x - 2$	$y$
-2	$-(-2) - 2 = 0$	0
-1	$-(-1) - 2 = -1$	-1
0	$-(0) - 2 = -2$	-2

*Coordinates: (-2, 0), (-1, -1), (0, -2)*

$$\begin{array}{r} -5y + 5x = 10 \\ -5x \quad -5x \\ \hline 5y = -5x + 10 \\ \div 5 \quad \div 5 \\ \hline y = -x + 2 \end{array}$$

*$y = mx + b$*   
*↑ slope ↑ y-int.*

$$\begin{array}{r} -5y + 5x = 10 \\ -5y \quad -5y \\ \hline 5x = 10 \\ \div 5 \quad \div 5 \\ \hline x = 2 \end{array}$$

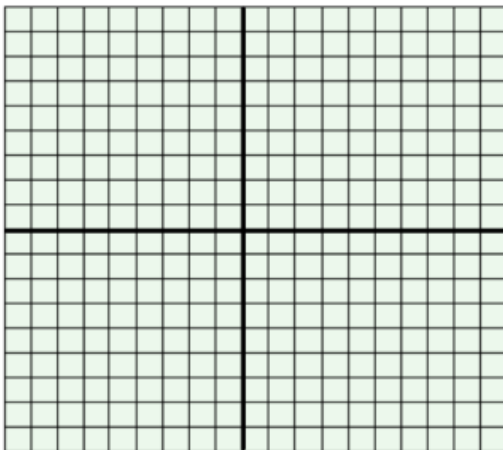
$$\begin{array}{r} y + x = -2 \\ -x \quad -x \\ \hline y = -2 \end{array}$$

*$y = x - 2$*



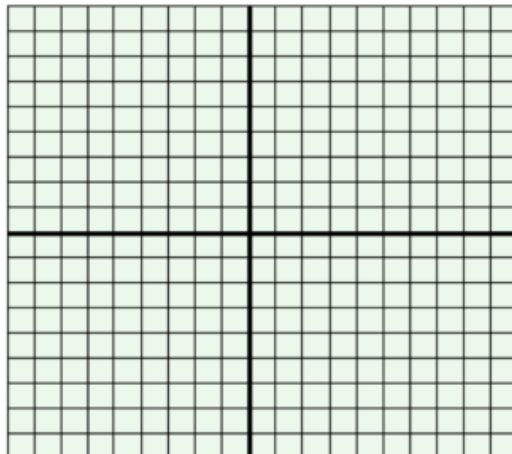
3. Graph the following equations. Determine if the data is either discrete or continuous.

$$y = 2x + 3 \quad x, y \in \mathbb{I}$$



✓ r

$$y + 5x = 7 \quad x, y \in \mathbb{R}$$



$$= 7 + 10 = 17$$

Pg. 96 here

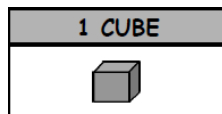
Focus A Pg 97.

### Investigation #1:

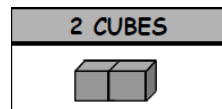
Finding a Pattern: we will use a pattern to make predictions about trains constructed from cubes.

#### Together As a Class.....


A. Place one cube on the desk. How many faces are visible?



B. Use two cubes to make a train on the desk. How many faces are visible?



C. Create more trains. Each train will have one cube more than the previous train. Record the number of visible faces on each train.

3 CUBES	Number of Cubes	1	2	3	4	5	6	7
	Number of Visible Faces	5						

What pattern do you see in the sequence of numbers you collected?

**sequence** = a set of numbers arranged in order according to a pattern or rule.

### Investigation Questions:

1. How many visible faces are there for a train of 11 cubes?
2. What is the number of visible faces for a train of 12 cubes and for a train of 15 cubes?
3. List restrictions on possible values for the number of visible cubes.
4. Predict the number of visible faces for a train of 200 cubes.

## Class work / Homework:

Complete the following:

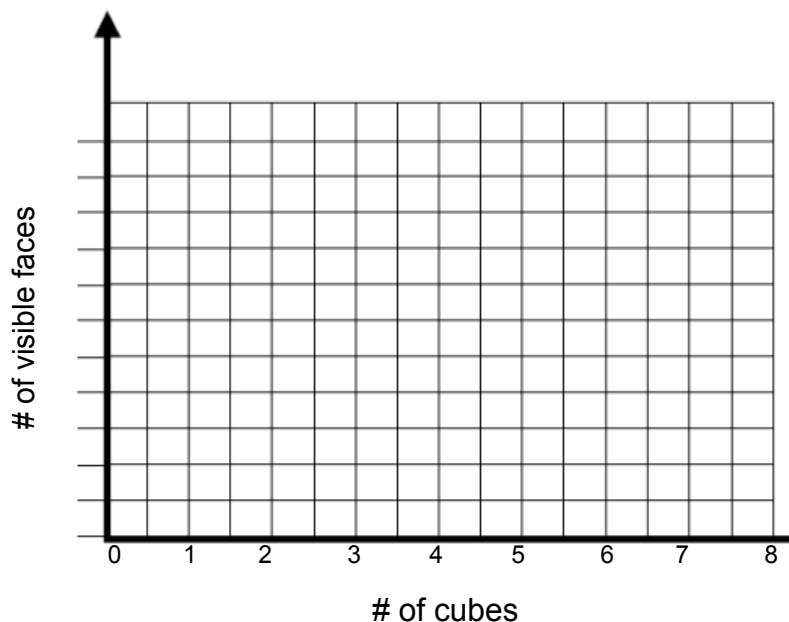
- Focus A - A, B, C (write the set notation for the domain and range), and D
- Focus Questions 5, 6, 7, 8 a, and 9
- Check your Understanding 13, 14, 16

## Answers:

- Focus A:

A. On Cartesian plane, graph the table of values from Investigation #1:

Number of Cubes	1	2	3	4	5	6	7
Number of Visible Faces	5	8	11	14	17	20	23



B. Should you join the points on the graph (determine whether the data are continuous or discrete)?

C. Write the set notation for domain and for the range.

D. Describe the patterns shown on the graph:

a) geometric pattern

b) display of patterns from the table of values

c) why are all the points in the first quadrant

• **Focus Questions:**

5. a) Use your graph to find the number of visible faces for a train with 18 cubes.

b) Explain how you found your answer. Is a graph the best way to do this? Explain.

c) How confident are you that your answer is correct?

6. What is the most reasonable way to find the number of visible faces for a train of 200 cubes? Explain.

7. Is it easier to use a graph or a table of values to make predictions for a large number of cubes? Explain.

8. Suppose you were asked to find the number of visible faces for a train with 1000 cubes.

a) Explain why it would not be practical to use a cube model, table of values, or graph to find the number of visible faces.

9. Look at the pattern in the trains. Find the number of visible faces for each of the following trains.

a) 22 cubes

b) 30 cubes

c) 40 cubes

d) 50 cubes

e) 60 cubes

f) 70 cubes

13. a)

b)  $(2, 5) - A$

$(0, 1) - B$

$(0, 4) - C$

$(4, 2) - D$

c) A linear graph is like a non-linear graph in that they both have a pattern. They are different because a linear graph has coordinates that are in a line.

d)  $\textcircled{A} \{x \mid x = -8, -6, -2, \dots, x \in \mathbb{I}\}$   
 $\{y \mid y = -5, -2, \dots, y \in \mathbb{I}\}$

$\textcircled{D} \{x \mid x = 4, x \in \mathbb{W}\}$

e) Discrete

14.

13. a)

b) A - (-4, -1)

B - (7, -3)

C - (0, 4)

D - (4, 2)

c) A linear graph is like a non-linear graph in that it also has a pattern. It is different because a linear graph has coordinates that go in a line.

d) A)  $\{x \mid x = -6, -2, 0, 4, x \in \mathbb{I}\}$   
 $\{y \mid y = -3, 1, 3, 7, y \in \mathbb{I}\}$

e) discrete

D)  $\{x \mid x = 4, x \in \mathbb{W}\}$

14) a) increases by 0.5

c)  $\{x \mid x \geq 0, x \in \mathbb{R}\}$

## Creating Equations Terminology:

- Sum
- Product
- Difference
- Plus
- Doubled
- The result is
- Is the same as
- Tripled
- Diminished by
- Quotient
- Decreased by
- Take a half
- Trebled

### Creating Equations Examples:

- a) a number increased by 8.

$$n + 8$$

- b) John's age 3 years from now.

$$J + 3$$

- c) Three times the volume decreased by 10.

$$3v - 10$$

- d) The value, in cents, of x nickels.

$$0.05x$$

- e) One-half of the age Susan was 2 years ago.

$$\frac{(s-2)}{2}$$

### Creating Equations:

1. Three times a number.
2. A number increased by 4.
3. A number decreased by 3.
4. The length increased by 5m.
5. Mary's age 2 years ago.  $m - 2$
6. John's age 5 years from now.
7. Twice the width increased by 3.
8. One-half the speed.
9. Eight points less than the winner.  $w - 8$
10. Three times the volume decreased by 20.
11. The value, in cents, of x quarters.  $0.25x$
12. One third of Tom's age 10 years from now.  $\frac{(t+10)}{3}$
13. Six times a number decreased by 2.
14. Four times as many people.
15. Twice a number decreased by 7 equals 41.  $2n - 7 = 41$
16. 19 is subtracted from 3 times a number and the result is -1.
17. When a number is multiplied by 7, and 35 is subtracted from the product, the result is 59.

Pg. 101  
#16, 18

18. If you add 19 to a number the sum is the same as if you add 7 to twice the number.
19. Five times a number plus 19 equals nine times the number minus 41.
20. Three times a number is 45.
21. One-half of a number is 16.
22. Five times a certain number is 45.
23. If a number is doubled and 3 added, the result is 25.
24. If 8 is subtracted from  $\frac{3}{4}$  of a certain number, the result is 7.
25. When I double a certain number and add 16, the result is 40.
26. The number of pupils in a class is 33 and the number of boys is 7 greater than the number of girls.
27. If 37 is added to a certain number, the sum is 53.
28. If 27 is subtracted from a number, the result is 5.
29. When a number is multiplied by 7 and 25 subtracted from the product, the result is 59.
30. If five times a number is increased by 6, the sum is the same as if twice the number were increased by 15.
31. If you add 19 to a certain number the sum is the same as if you add 7 to twice the number.

### Investigation #3:

#### Problem

After researching the rates of different Internet providers, Daniella decided to use Company A. Company A charges \$20.00 per month plus \$2.00 per hour. Daniella's first monthly bill was \$80.00. How many hours was she on-line in the first month?

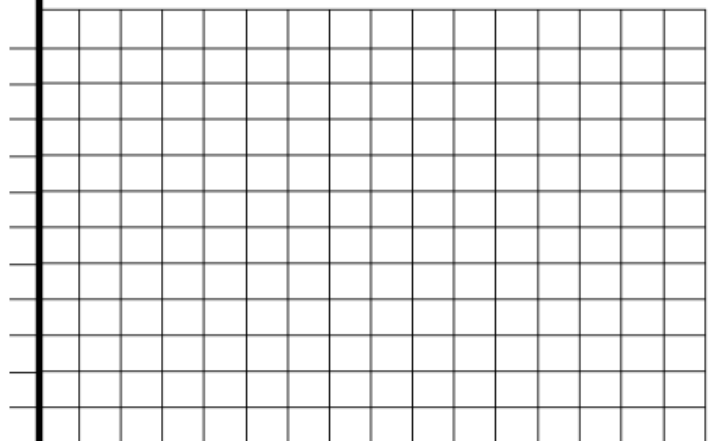
1. Determine the cost of using the internet by completing the table below.

2. Create a graph using the data from the table of values.

Hours (h)	Cost (C)
0	
1	
2	
3	
4	
5	
6	

a) What is the independent variable? \_\_\_\_\_

b) What is the dependent variable? \_\_\_\_\_





Fill in the table below with the appropriate information pertaining to the graph above.

	Continuous or Discrete Data?	Independent or Dependent Variable?	Domain or Range?
Time in hours (t)			
Total Cost in \$ (c)			

a) Describe the Domain and Range.

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3) Write a formula (using words) to find the cost of Internet use if the number of hours used in one month is known.

*Total Monthly Charge =*

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4) Write an equation (variables and numbers) to show the number of hours of Internet use for Daniella's bill of \$80.00.

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**Equation** = a mathematical sentence showing that expressions are equal in value. The variables are represented by letters.

## Warm-up#12

1. How are linear and non-linear graphs alike? How are they different?

patterns

Linear  
↳ line

2. Write the expression for each of the following:

a. 10 more than five times a number  $10 + 5n$  or  $5n + 10$

b. Helen's age 2 years ago  $h - 2$

c. One fourth of a number which has been increased by three  $\frac{1}{4}(n+3)$

d. When a number is multiplied by 6, and 25 is subtracted from the product, the result is 43.

$$6n - 25 = 43$$

### Example #1: Making an Equation

Ralph rents snow boards for \$3.50 per hour, but requires a \$2.00 non-refundable deposit. How much money will it cost you to rent Ralph's snow board and use it for 2 hours? How about 3 hours, 6 hours?

$$\begin{aligned}C &= 3.50h + 2.00 \\C &= 3.50(2) + 2.00 \\&\rightarrow C = 7.00 + 2.00 \\C &= 9.00\end{aligned}$$

\$9.00

- 1) must figure out what we are looking to solve for, and give it a letter.
- 2) must then write out how that solution is to be discovered.
- 3) must then make it into a formula that will be useable for any finding.
- 4) The equation should then be tested. Try to solve for 3, 6, and 10 hours.

### Practice:

Page 101, Question #18

An Internet provider charges \$20.00 ~~per~~ month plus \$2.00 for each hour of use. After how many hours would you be charged \$60.00 for the use of the Internet? Show all of your work.

$$\begin{aligned}C &= 20.00 + 2.00h \\C &= 2.00h + 20.00 \\60.00 &= 2.00h + 20.00 \\-20 &\quad -20 \\40 &= 2h \\ \frac{40}{2} &= \frac{2h}{2} \\20 &= h\end{aligned}$$

20 hrs.

- 1) must figure out what we are looking to solve for, and give it a letter.
- 2) must then write out how that solution is to be discovered.
- 3) must then make it into a formula that will be useable for any finding.
- 4) The equation should then be tested. Try to solve for how many hours you would have used the Internet to be charged \$60.00.

#16

Pg 101

$$a) C = 20 + 6p$$

$$C = 20 + 6(10)$$

$$C = 20 + 60$$

$$C = 80 \quad \$80.00$$

$$b) C = 20 + 6p$$

$$100 = 20 + 6p$$

$$\begin{array}{r} -20 \\ \hline \end{array}$$

$$\frac{80}{6} = \frac{6p}{6}$$

$$13.3 = p$$

13 photos

Pg. 102 #20-24

$$20) a) C = 200 + 50h$$

$$b) 525 = 200 + 50h$$

$$\begin{array}{r} -200 \\ \hline \end{array}$$

$$\frac{325}{50} = \frac{50h}{50}$$

6 1/2 hours

$$h = 6.5 \text{ hours}$$

$$21) E = 10000 + 2c$$

$$a) E = 10000 + 2(50000)$$

$$E = 10000 + 100000$$

$$E = \$110000$$

$$b) E = 10000 + 2c$$

$$40000 = 10000 + 2c$$

$$\begin{array}{r} -10000 \\ \hline \end{array}$$

$$\frac{30000}{2} = \frac{2c}{2}$$

$$c = 15000 \text{ cds}$$

$$22) \downarrow E = 2.50c \downarrow$$

$$b) E = 2.50(50000)$$

$$E = \$125000$$

## Class work / Homework:

Complete the following:

- Check Your Understanding pg. 102  
#s ~~19~~, 20, 21, 22<sup>bc</sup>, 23, 24, ~~25 (a and c)~~

20-24

Pg. 102 #20

$$C = 200 + 50h$$

$$525 = 200 + 50h$$

$$\begin{array}{r} 525 \\ -200 \\ \hline \end{array}$$

$$\frac{325}{50} = \frac{50h}{50}$$

6 1/2 hours

$$h = 6.5$$

21.  $E = 10,000 + 2c$

a)  $E = 10,000 + 2(50,000)$

$$E = 10,000 + 100,000$$

$$E = \$110,000$$

b)  $E = 10,000 + 2c$

$$\begin{array}{r} 40,000 = 10,000 + 2c \\ -10,000 \quad -10,000 \\ \hline \end{array}$$

$$\frac{30,000}{2} = \frac{2c}{2}$$

$$c = 15,000$$

cap

(cds)

22.  $E = 2.5c$

b)  $E = 2.5c$

$$E = 2.5(50,000)$$

$$E = \$125,000$$

c)  $E = 2.5c$

$$\frac{40,000}{2.5} = \frac{2.5c}{2.5}$$

$$c = 16,000 \text{ cds}$$

# Warm - Up

Read Question #24 Pg. 102 and then do the following:

1. Make an equation
2. Answer (a)
3. Make a table of values
4. Graph the coordinates (does not have to be done on graph paper)
5. Question: Should you join the dots on your graph?
6. Question: Is the data discrete or continuous?
7. State the domain and range
8. Question: What is the geometric pattern?

Please be ready to switch warm-up books

$$1) C = 3 + 0.5k$$

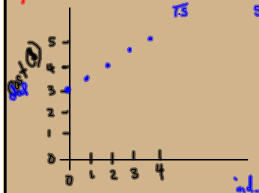
$$2) 32 = 3 + 0.5k$$

$$\begin{array}{r} -3 \quad -3 \\ \hline 29 = 0.5k \\ 0.5 \quad 0.5 \\ \hline k = 58 \end{array}$$

58 km

$$3) \begin{array}{c|c} k & C \\ \hline 0 & 3 + 0.5(0) \\ 1 & 3 + 0.5(1) \\ 2 & 3 + 0.5(2) \\ 3 & 3 + 0.5(3) \\ 4 & 3 + 0.5(4) \end{array}$$

$$4) (0,3) (1,3.5) (2,4) (3,4.5) (4,5)$$



5) Saying yes or connecting the dots

6) continuous Number of km

$$7) \text{domain } \{k | k \geq 0, k \in \mathbb{R}\}$$

$$\text{range } \{C | C \geq 3, C \in \mathbb{R}\}$$

8) Linear

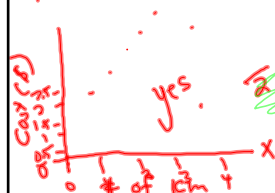
$$y = 3 + 0.50x$$

$$C = 0.50x + 3$$

$$(a) 32 = 0.5x$$

$$\begin{array}{r} -3 \quad -3 \\ \hline 29 = 0.5x \\ 0.5 \quad 0.5 \\ \hline x = 58 \end{array}$$

The distance was 58 km

$$\begin{array}{c|c} x & y = 0.5x + 3 \\ \hline 0 & 0.5(0) + 3 \\ 1 & 0.5(1) + 3 \\ 2 & 0.5(2) + 3 \\ 3 & 0.5(3) + 3 \\ 4 & 0.5(4) + 3 \end{array}$$


$$\text{domain } \{x | x = 0, 1, 2, 3, 4\}$$

$$\text{range } \{y | y = 3, 3.5, 4, 4.5, 5\}$$

Continuous

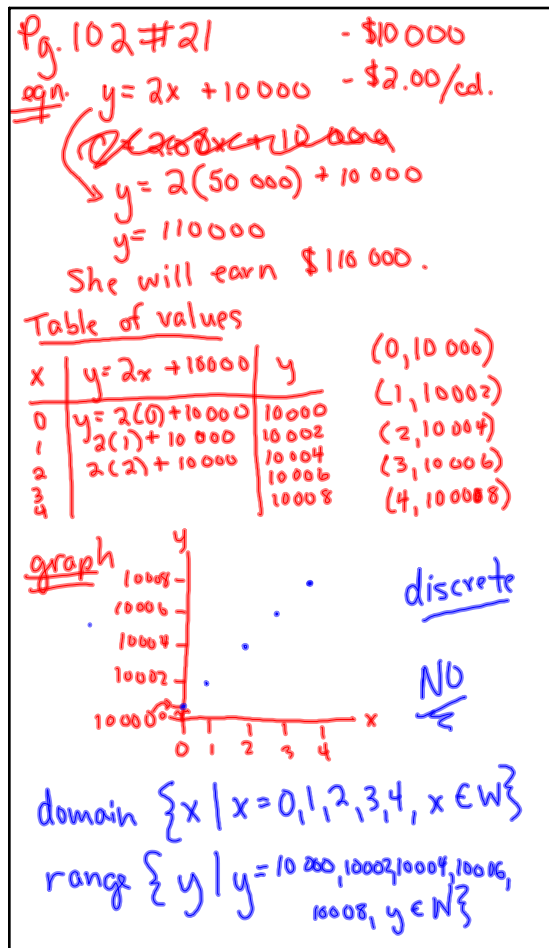
Write an equation to represent each of the following situations:

a) Your neighbor pays \$5 per hour to their babysitter.

If  $t$  = total amount made and  $x$  = number of hours you were babysitting, what would the equation look like?

b) Greco delivers pizza for \$5 flat fee and \$8 per medium pizzas ordered. If  $t$  = total amount and  $x$  = number of medium pizzas, what would the equation look like?

c) Standard Taxi charges \$4 pick up fee and \$1.25 per kilometer. If  $t$  = total amount and  $x$  = number of kilometers driven, what would the equation look like?



## Quiz Thursday - Section 3.1

- Number Term.  $(R, Q, \bar{Q}, I, W, N)$

- Graphing on a number line

- open or closed dots

- a line or dots

- Table of values

- graphed coordinates  $(x, y)$

- discrete or continuous data

- join the dots on graph? if its continuous

- domain and range

domain  $\{x = 0, 1, 2, \dots\}$

range  $\{y = 1, 2, 5, y \in \mathbb{N}\}$

$(0, 1) (0, 5)$   
 $(1, 2) (3, 5)$

- creating an equation

- Word Problems  $\rightarrow$  make an eqn. and solve it

$\rightarrow$  equation

$$C = 2x + 5$$

$\hookrightarrow$  table of values

$\hookrightarrow$  graph

$\hookrightarrow$  discrete or continuous  
 $\rightarrow$  join the dots?

$\hookrightarrow$  domain + range

$\hookrightarrow$  Geo.  
Linear

Attachments

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Domain, Range, Continuous & Discrete worksheet #2.doc